

Bulk Physics at a Graviton Factory*

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Abstract

A general prediction of the 5-d Randall-Sundrum (RS) hierarchy model is the emergence of spin-2 Kaluza Klein (KK) gravitons with weak scale masses and couplings. The lowest order effective theory of the RS model is given by 5-d Einstein gravity which uniquely fixes the self-interactions of gravitons. We demonstrate that large numbers of light KK resonances could be produced at a future lepton-collider-based “Graviton Factory”. Measuring the self-interactions of these KK gravitons will probe the accuracy of the 5-d Einstein gravity picture and, in addition, yield indirect information on the as yet untested self-coupling of the 4-d graviton. The self-interactions of the gravitons can be studied by measuring the decays of the heavier states to the lighter ones. Using the AdS/CFT picture, these can be interpreted as the decays of heavier resonances to lighter ones, in a strongly coupled 4-d CFT. We show that these decays have sufficient rates to be studied at future colliders and that they are also, in principle, sensitive to higher derivative operators, such as the Gauss-Bonnet term. In a generalized RS model, with non-universal 5-d fermion masses, FCNC’s will be induced. We show that precise measurements of the rare decays of KK graviton/gauge states into flavor non-diagonal final states at a Graviton Factory can be used to map the 5-d fermion mass matrix.

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1 Introduction

The Randall-Sundrum (RS) model offers an interesting geometric view of the hierarchy between the apparent scale of gravity $\overline{M}_P \sim 10^{18}$ GeV and the weak scale $M_w \sim 10^2$ GeV [1]. The RS model background geometry is AdS_5 (5-d spacetime with constant negative curvature), truncated by two 4-d Minkowski walls separated by a fixed distance. All the parameters of the model are assumed to be naturally given by various powers of the 5-d fundamental scale $M_5 \sim \overline{M}_P$. In the original RS construct, the Standard Model (SM) fields are confined to one of the 4-d boundaries which we will refer to as the SM wall. The induced metric on the SM wall then generates from M_5 a physical scale $\Lambda_\pi \sim M_w$, through a geometric exponential warp factor. Due to this exponentiation, no large hierarchies need to be introduced; for more details on the RS construct please see Ref. [1].

A generic prediction of the RS model is the emergence of spin-2 resonances $G^{(n)}$, $n = 1, 2, 3, \dots$, which are the Kaluza-Klein (KK) excitations of the 5-d graviton. The masses and couplings of $G^{(n)}$ are set by Λ_π , and hence, these resonances could be relevant to physics at the weak scale. Many recent works have studied the phenomenological effect of $G^{(n)}$ on collider and precision electroweak data [2]. These studies have focused on the leading coupling of $G^{(n)}$ to the SM field content. The RS model is based on an effective 5-d Einstein Gravity (EG_5) theory which describes the coupling of the graviton to the SM fields, as well as its self-couplings. The $G^{(n)}$ are the 4-d manifestations of the 5-d graviton. Hence, to test the model at leading order, one must go beyond the $G^{(n)}$ –SM coupling and also probe the leading order inter-couplings of $G^{(n)}$ which are fixed, given Λ_π from collider data. This is similar to testing QCD at tree level, which requires agreement between theory and experiment, not only for the quark-gluon coupling, but also for the gluon self-couplings. The inter-couplings of $G^{(n)}$ can also yield indirect evidence for the as yet unobserved massless 4-d graviton self-coupling, as well as a handle on the coefficients of possible 5-d higher derivative terms, such as the Gauss-Bonnet term.

The original RS model has also been generalized to allow for the SM fields to reside in the 5-d bulk. An important set of parameters that enters this generalized RS model is the 5-d mass matrix of the SM bulk fermions. It has been shown that the value ν of the 5-d fermion mass in units of k , where k is the curvature scale of

AdS₅, has a significant role in the low energy phenomenology of the model [3], since it controls the couplings of the zero mode (observed) fermion to $G^{(n)}$ and the KK gauge fields $A^{(n)}$. It has been pointed out that giving various flavors of fermions different 5-d masses induces FCNC's at tree level [4]. Thus, these masses must be fairly universal in order to avoid unacceptably large FCNC's. One way of probing the 5-d fermion mass matrix is to search for presumably rare flavor non-diagonal decays of $G^{(n)}$ and $A^{(n)}$.

To probe graviton self-coupling or the 5-d masses of the fermions with precision in the aforementioned manner, a large number of KK excitations are needed. In this paper, we show that if a generic RS-type model is realized in Nature an appropriate weak scale Linear Collider (LC) can be used to produce large numbers, $\sim 10^7$, of light KK gravitons. In this sense, the LC can operate as a ‘‘Graviton Factory’’. Of course, if the SM fields reside in the 5-d bulk, we expect to produce comparably large numbers of light KK gauge fields as well.

As an example of the $G^{(n)}$ inter-coupling, we study the decay $G^{(3)} \rightarrow G^{(1)}G^{(1)}$, which is the first kinematically allowed decay within the graviton sector. We give the branching fraction for this decay as a function of the ratio of the masses in the initial and final states; it is found that the dependence on the mass ratio is fairly strong. However, at the classical level in the RS model, the mass ratio is fixed by the geometry and the branching fraction for $G^{(3)} \rightarrow G^{(1)}G^{(1)}$ is about 15%. These results are presented in section 2, where brief comments on the AdS/CFT [5] interpretation of such decays and the effect of 5-d higher derivative terms are also included.

In section 3, we study a model in which all SM fermions except the top quark will be assumed to have the same value of ν . We then show the effects of this mass matrix in terms of flavor non-diagonal decays of $G^{(1)}$ and $A^{(1)}$. Although this model is perhaps too simplistic to be phenomenologically relevant, it demonstrates the utility of studying such decays at future Graviton Factories in probing the bulk fermion mass matrix. Some concluding remarks are presented in section 4.

2 Graviton Sector Self-Interactions

As mentioned before, the RS model generically predicts the emergence of spin-2 KK gravitons $G^{(n)}$ in the 4-d effective theory. The equations of motion for $G^{(n)}$ are

obtained through the KK reduction of the EG_5 action S_G , containing the 5-d graviton kinetic term. We have

$$S_G = 2 M_5^3 \int d^5x \sqrt{-G} R_5, \quad (1)$$

where $G = \det(G_{\mu\nu})$, $G_{\mu\nu}$ is the RS background metric, and R_5 is the 5-d Ricci scalar. The 4-d interactions of the $G^{(n)}$ states with the SM fields are given by the following Lagrangian

$$\mathcal{L}_{SM} = - \left[\frac{1}{\overline{M}_P} h_{\mu\nu}^{(0)} + \frac{1}{\Lambda_\pi} \sum_{n=1}^{\infty} h_{\mu\nu}^{(n)} \right] T^{\mu\nu}, \quad (2)$$

where the 4-d tensor fields $h_{\mu\nu}^{(n)}$ represent the $G^{(n)}$ states, and $T^{\mu\nu}$ is the energy momentum tensor of SM which is assumed to reside on the SM wall, in Eq. (2). Phenomenological studies of the RS model have so far focused on the interactions coming from \mathcal{L}_{SM} , such as the on-shell decays of $G^{(n)}$ into SM fields. These interactions are only suppressed by one power of Λ_π for $n = 1, 2, 3, \dots$

However, there are also interactions amongst $G^{(n)}$, resulting from the KK reduction of the self-coupling of the 5-d graviton in S_G . In powers of M_5^{-1} , the leading 5-d self-coupling is the triple graviton vertex. This indicates that in 4-d the $\{G^{(l)}, G^{(m)}, G^{(n)}\}$ coupling is, in powers of Λ_π^{-1} , the leading interaction in the KK graviton sector. This can be seen by using the KK graviton wavefunctions [6], and inspecting the triple KK graviton coupling of S_G . Thus, to test the RS model to leading order in Λ_π^{-1} , one must also study the $\{G^{(l)}, G^{(m)}, G^{(n)}\}$ couplings. We note that quartic couplings of the $G^{(n)}$ are higher order in Λ_π^{-1} , as they are for the 5-d graviton in powers of M_5^{-1} . In principle, there could be higher derivative terms, such as R_5^2 , in the 5-d theory. However, their contribution to the $\{G^{(l)}, G^{(m)}, G^{(n)}\}$ couplings are higher order in Λ_π^{-1} . We will briefly discuss the R_5^2 terms at the end of this section.

In the following, we study the process $G^{(3)} \rightarrow G^{(1)}G^{(1)}$ which is the first kinematically allowed two body decay in the KK sector. To do this, we need the triple graviton vertex. This vertex has the same tensor structure regardless of the number of dimensions and the background geometry. Hence, we use the Feynman rules of Ref. [7] for the 3-graviton vertex $V_{\{\mu_i, \nu_i\}}(K_i)$, $i = 1, 2, 3$, where $\{\mu_i, \nu_i\}$ are 4-d Lorentz indices and K_i is the 4-momentum of the particle labeled i , in Ref. [7]. Since $V_{\{\mu_i, \nu_i\}}(K_i)$ has the same tensor structure in 5-d, we use the same function for the 5-d graviton triple coupling, and treat $\{\mu_i, \nu_i\}$ and K_i as 5-dimensional. To get the decay rate for $G^{(3)} \rightarrow G^{(1)}G^{(1)}$, we must square $V_{\{\mu_i, \nu_i\}}(K_i)$ and contract it with the

product of three massive graviton polarization sums, to project out the appropriate degrees of freedom. This sum is given in Ref. [8] for the case of flat extra dimensions. However, the degrees of freedom of the 4-d KK gravitons are the same for the RS and the flat cases, independent of the higher dimensional theory.

The amplitude for the on-shell decay is obtained when the vertex is contracted with the 4-d massive spin-2 polarization vectors of the KK states. In this way, we see that the only relevant indices are 4-d and we can take $\{\mu_i, \nu_i\}$ to be 4-d Minkowskian. However, the scalar products of the 5-momenta, $K_i \cdot K_j$, in $V_{\{\mu_i, \nu_i\}}(K_i)$ must be treated carefully. By using the 4-d massive graviton polarization sum we have extracted the appropriate tensor structure, but to complete the reduction from 5-d to 4-d, these scalar products should be expressed in terms of 4-d quantities. The 5-momenta K_i^M , $M = 0, 1, \dots, 4$, in the Feynman rules correspond to 5-d derivatives ∂^M , acting on the graviton field h_i . Thus, $K_i \cdot K_j$ corresponds to terms proportional to $G^{MN} \partial_M h_i \partial_N h_j$, in the 5-d action.

The 5-d graviton can be expanded in the KK modes $h_{\mu\nu}^{(n)}$

$$h_{\mu\nu}(x, \phi) = \sum_{n=0}^{\infty} h_{\mu\nu}^{(n)}(x) \frac{e^{-2\sigma} \chi^{(n)}(\phi)}{\sqrt{r_c}}, \quad (3)$$

where the Z_2 even wavefunctions $\chi^{(n)}(\phi)$ only depend on the 5th dimension parameterized by $\phi \in [-\pi, \pi]$; $x^4 = r_c \phi$, $\sigma = kr_c |\phi|$, and $r_c \sim 10 k^{-1}$ is the compactification radius. Note that, in Eq. (3), the graviton is taken to be a 5-d tensor fluctuation on the AdS_5 background. The 4-d derivatives ∂_μ do not act on $e^{-2\sigma} \chi^{(n)}(\phi)$ and thus, after integration over the extra dimension, the 4-d part of the dot product $K_i \cdot K_j$ is an overall constant times the 4-d Minkowski scalar product, for a given vertex with fixed KK fields. However, ∂_ϕ acts on $e^{-2\sigma} \chi^{(n)}(\phi)$ and, hence, the 5-d part of $K_i \cdot K_j$ depends on the mode number n of the KK states whose momenta are K_i and K_j . Therefore, for particles $\{G_i^{(m)}, G_j^{(n)}\}$, we may schematically write

$$\int d\phi K_i \cdot K_j \rightarrow \alpha k_i \cdot k_j - \beta_{ij}(m, n), \quad (4)$$

where k_i are the Minkowski 4-momenta. We again note that α does not depend on the mode numbers (m, n) of the particles whose momenta are in the product, but $\beta(m, n)$ does. That is, for the 4-d parts of the vertex, such as the terms proportional to $k_i \cdot k_j$, α is the same and is given by integrating the wavefunctions $\chi^{(n)}(\phi)$ for

the particles in the vertex, say $\{G^{(l)}, G^{(m)}, G^{(n)}\}$, over the extra dimension. However, $\beta(m, n)$ are given by integrating a product proportional to $\chi^{(l)} \partial_\phi \chi^{(m)} \partial_\phi \chi^{(n)}$, which depends on the modes (m, n) .

Using the notation of Ref. [6], we have

$$\chi^{(n)} \simeq \frac{e^{2\sigma}}{N_n} J_2(z_n), \quad (5)$$

where J_l is the l^{th} order Bessel function. The normalization is given by

$$N_n \simeq \frac{e^{kr_c\pi}}{\sqrt{kr_c}} J_2(x_n), \quad (6)$$

where $J_1(x_n) = 0$; $z_n = (m_n/k)e^\sigma$, and m_n is the mass of the n^{th} KK graviton. Given $\chi^{(n)}$ from Eq. (5), integration of the $\{G^{(l)}, G^{(m)}, G^{(n)}\}$ vertex in S_G of Eq. (1) over the extra dimension yields

$$\alpha = \lambda_1 \int_{-\pi}^{\pi} d\phi e^{4\sigma} J_2(z_l) J_2(z_m) J_2(z_n), \quad (7)$$

where

$$\lambda_1 = \frac{(2\overline{M}_P)^{-1} kr_c e^{-3kr_c\pi}}{J_2(x_l) J_2(x_m) J_2(x_n)}. \quad (8)$$

We also obtain

$$\beta(m, n) = \lambda_2 \int_{-\pi}^{\pi} d\phi e^{4\sigma} J_2(z_l) J_1(z_m) J_1(z_n), \quad (9)$$

where

$$\lambda_2 = m_m m_n \lambda_1. \quad (10)$$

In getting our results, we have ignored terms that come from the action of ∂_ϕ on the background metric $G_{\mu\nu} = e^{-2\sigma} \eta_{\mu\nu}$ or the prefactor $e^{-2\sigma}$ of the 5-d graviton wavefunction in Eq. (3). These terms, after integration by parts, are proportional to $(\sigma')^2$, where $\sigma' \equiv \partial_\phi \sigma$. The terms proportional to $(\sigma')^2$ come with no derivatives on the $\chi^{(n)}$ -fields and thus would yield anomalous contributions to the 4-d Minkowski couplings of the zero-mode graviton on the SM wall. Hence, to maintain the RS construct, they must cancel out, presumably after including the 5-d Cosmological Constant term contributions to the triple graviton vertex.

Here, we note that the overall coefficient of the vertex $\{G^{(l)}, G^{(m)}, G^{(n)}\}$ has been fixed by comparing the KK zero mode contribution to the vertex and matching with the 4-d results of Ref. [7], after integrating over the extra dimension. We may now

numerically compute the decay rate for $G^{(3)} \rightarrow G^{(1)}G^{(1)}$. The branching ratio for the decay as a function of m_1/m_3 is presented in Fig. (1). Of course, at the classical level in the RS model, $m_1/m_3 \simeq 3.83/10.17$, for which the branching fraction is about 15%. However, if the mass ratio is slightly different, perhaps due to quantum effects, the change in the branching ratio is not negligible, as seen in Fig. (1). Higher KK modes may decay into more than two $G^{(n)}$ resonances, *e.g.*, $G^{(n+1)} \rightarrow nG^{(1)}$. However, such decays come from Feynman diagrams that are higher order in Λ_π^{-1} . In addition, perturbative calculations are unreliable at scales much higher than Λ_π .

In an AdS/CFT picture [9], the KK states $G^{(n)}$ correspond to the resonances of a strongly coupled 4-d CFT. Thus, decays such as $G^{(3)} \rightarrow G^{(1)}G^{(1)}$ can be thought of as the decays of heavier CFT resonances to lighter ones. In the context of a CFT, there are $\sim c^{-1}$ “narrow” resonances, where $c \equiv k/\overline{M}_P$, corresponding to the lightest $G^{(n)}$ states, for $n \lesssim c^{-1}$. Again, the CFT states with masses much larger than Λ_π are too broad to be considered single resonances, and the computations based on the particle picture of the $G^{(n)}$ are no longer adequate.

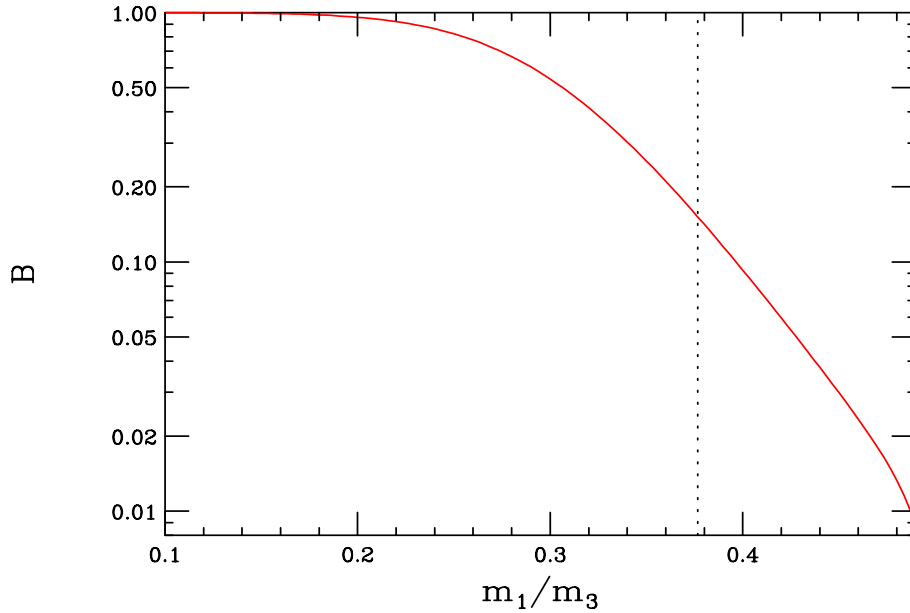


Figure 1: Branching fraction for the decay $G^{(3)} \rightarrow G^{(1)}G^{(1)}$ as a function of the mass ratio m_1/m_3 assuming $m_3 = 2$ TeV. The fixed value of this ratio in the RS model is shown as the dotted line and yields $B \simeq 15\%$.

Here we note that the decay $G^{(3)} \rightarrow G^{(1)}G^{(1)}$ can also get contributions from higher derivative operators proportional to R_5^2 , such as the 5-d Gauss-Bonnet term. These contributions will be parametrically non-leading, as the associated vertices are suppressed by $c^{-2/3}\Lambda_\pi^{-3}$. One finds their relative contributions to the decay rate for $G^{(3)} \rightarrow G^{(1)}G^{(1)}$ to be $\sim (c^{1/3}x_3)^2$ where $x_3 \simeq 10.1735$. Thus, even if $c \ll 1$ these terms may have a large effect, assuming that their coefficients in the 5-d action are not too small. This allows for the possibility of measuring the 5-d R_5^2 coefficients of the theory at the 1% level from measurements of $G^{(n)}$ decays in future experiments, once the RS resonances are discovered. In the case where the $G^{(n)}$ have decays to three or more final state gravitons the presence of the R_5^2 -like terms will lead to a distortion of the final state spectrum thus providing a further handle on their relative contribution beyond the total rate.

Probing the RS KK graviton sector and the bulk fermion mass matrix with precision, as discussed in this and the next sections, requires large numbers of events. Here, we note that a future LC will have ample data to achieve such precise measurements. To see this, consider the cross section for $e^+e^- \rightarrow \mu^+\mu^-$ for the case where the SM is on the wall. The branching fraction for μ pairs is $\simeq 0.02$ and the light KK resonance cross sections are $10^3 - 10^4 fb$ [6]. As the integrated luminosities of typical LC's are in the range of $100 - 500 fb^{-1}/yr$, it is clear that one should easily expect $\sim 10^7$ graviton resonances in the TeV range to be produced. Similar arguments apply when the SM lies in the bulk and $\nu > -0.5$ [10]. When $\nu < -0.5$ one can instead use $\gamma\gamma$ collisions to produce graviton resonances at rates of order $10^7/yr$.

3 Flavor Changing Decays of Bulk Fields

As described above, the large number of KK gravitons, $\sim 10^7$, produced at future lepton colliders will allow for a detailed study of their rare decay modes. We now consider the case where the SM fields reside in the 5-d bulk. Since the parameter ν controls the strength of the couplings of both the graviton and gauge KK towers to the zero mode fermions, allowing fermions with the same SM quantum numbers to have different values of ν leads to Flavor-Changing (FC) couplings as noted by several authors [4]. The observation of rare decays induced by FC couplings could then be

used to map out the 5-d fermion mass matrix. To be specific we consider a toy model where all of the fermions except the top quark have the same value of $\nu = -0.4$ and we let ν_t vary. (We choose the value $\nu = -0.4$ since it is middle of region III [10] where all of the lightest graviton and gauge KK excitations are observable at colliders and there are no hierarchically large values of Λ_π .) In this case, the mixing in the $Q = 2/3$ sector will generate FC u, c, t couplings which are somewhat less constrained than those in the $Q = -1/3$ sector [11]. Whether such FC couplings are sufficiently large as to be dangerous for low-energy D meson physics is beyond the scope of the present paper. In either case, the theory presented here is just a toy model for demonstration purposes and is not to be taken too seriously.

Let $c_i^{G,A}$ denote the couplings of a zero mode fermion, having $\nu = \nu_i$, to the lowest graviton or gauge excitation in the weak eigenstate basis, *i.e.*, $c_i^{G,A} = C_{001}^{f\bar{f}G,A}(\nu_i)$ using the notation in Ref. [10]. (Here, $i = 1, 2, 3$ will label the fields u, c and t .) Symbolically, we can write this interaction as $\bar{f}_i^{(0)} c_i^{G,A} f_i^{(0)} G^{(1)}, A^{(1)}$. Converting to the mass eigenstate basis by a unitary transformation U this becomes $\bar{f}_k^{(0)} U_{ki}^\dagger c_i^{G,A} U_{ij} f_j^{(0)} G^{(1)}, A^{(1)}$. Now consider the case $k = 3$ and $j = 1, 2$ and use the fact that $c_1^{G,A} = c_2^{G,A}$ together with the unitarity condition $\sum_i U_{ki}^\dagger U_{ij} = \delta_{kj}$; the strength of the FC couplings are found to be $(c_3^{G,A} - c_1^{G,A}) U_{33}^\dagger U_{31,2}$. The difference in the c_i can be obtained directly by performing some basic integrations over Bessel functions, once the value of ν_t is specified. To obtain sample numerical results we will assume that $U_{ij} \sim (V_{CKM})_{ij}$ at least qualitatively so that, *e.g.*, $U_{33} = 1$ and $U_{32} \simeq A\lambda^2 \simeq 0.04$. Note that in this toy model the $t\bar{c}$ coupling is thus expected to be an order of magnitude larger than the corresponding $t\bar{u}$ one.

It is now straightforward to obtain the desired branching fractions B for $G, A \rightarrow t\bar{x} + x\bar{t}$ which are shown in Fig. (2) as functions of $\Delta\nu = \nu_t - \nu$ with $\nu = -0.4$ assuming first KK masses of 1 TeV. (For the gauge boson KK case we assume that we are probing the almost degenerate first γ/Z excitation. Comparable results would be obtained for the first KK gluon excitation.) We see immediately that if $\Delta\nu$ is sizeable, *e.g.* $\Delta\nu \gtrsim 0.1$, branching fractions as large as $10^{-(3-4)}$ are obtainable. Decays at such high rates will be trivial to observe with a sample of $\sim 10^7$ gravitons or gauge KK excitations. For very small $\Delta\nu$ we find the approximate relations $B \simeq 1.4 \times 10^{-6} [\Delta\nu/0.01]^2$ for gravitons and $B \simeq 5.3 \times 10^{-6} [\Delta\nu/0.01]^2$ for neutral gauge bosons. Using these results it is clear that values of $|\Delta\nu| \sim 0.01$ can be probed through these

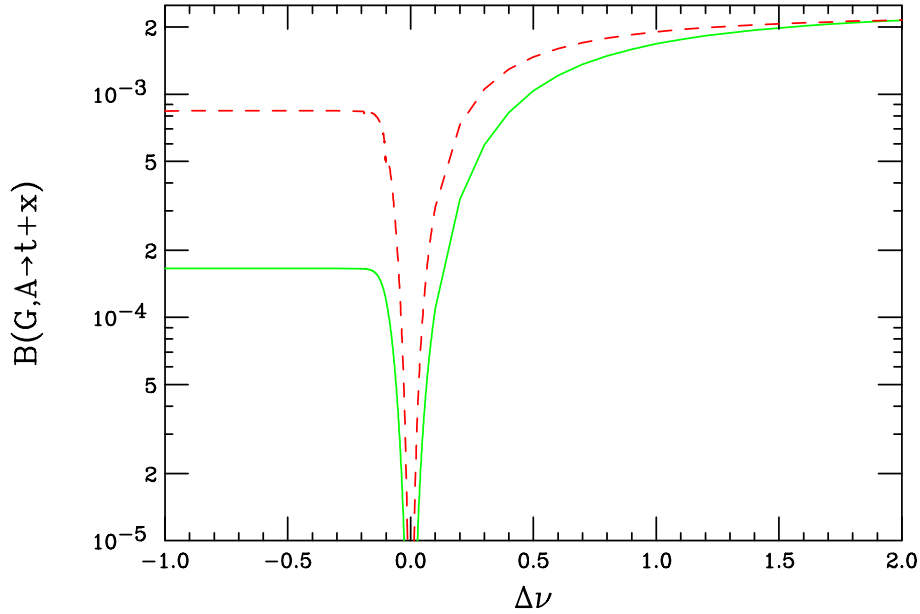


Figure 2: The flavor changing branching fractions for a 1 TeV first graviton (solid green) or γ/Z (dashed red) excitation as functions of $\Delta\nu$.

decays, at LC Graviton Factories.

4 Conclusion

In this paper we have explored some of the physics accessible at LC Graviton Factories which may produce as many as 10^7 resonant gravitons per year at design luminosities, depending upon their mass. We examined two particular processes: *(i)* the decay of a heavy graviton tower member into two lighter ones and *(ii)* the flavor changing decay of a light graviton (or bulk vector field) when the SM is off the wall.

As described in the text, the tree-level coupling of gravitons to matter occurs at the same order as does the trilinear graviton coupling, in analogy with QCD. In order to explore the underlying theory of gravity in the RS model, it is necessary to probe these gravitational self-couplings. This becomes possible in the RS model at Graviton Factories where we can observe the decay of higher KK states into lighter ones. We note that by the AdS/CFT correspondence, one could interpret these KK gravitons as the resonances of a strongly coupled 4-d CFT [9]. In particular, we examined the process $G^{(3)} \rightarrow G^{(1)}G^{(1)}$ which due to the RS particle spectrum is the

first accessible one at colliders. The branching fraction for this decay was found to be about 15%. This branching fraction yields a precise measurement of the gravitational self-interactions which allows us to probe, *e.g.*, higher derivative contribution in the 5-d action, such as the Gauss-Bonnet term, at the level of 1% or better. The decay rate shows sensitivity to m_1/m_3 ; this ratio could in principle receive quantum corrections.

In the case where the SM fields lie in the bulk, giving fermions of each generation with the same electroweak charges different values of the parameter ν leads to FCNC-type decays. If the branching fractions for these decays are precisely measured we can map out the values of ν for all the fermions. In this paper, we demonstrated, within the context of a toy model, that such FCNC's can be sizeable for both graviton and gauge KK resonances and that the precision measurements at a Graviton Factory can probe differences in ν values as low as 0.01. Together with ordinary flavor conserving decays, these can be used to map out all of the fermion locations in the extra dimension.

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